

# RANSAC = RANdOm SAmple Consensus

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*Courtesy: Ondřej Chum, Tomáš Svoboda*

## RANSAC informally

- ◆ Random sample consensus (RANSAC) is an iterative method estimating parameters of a (parametric) mathematical model from a set of observed data that contains outliers.
- ◆ Outliers should have no influence on the values of the estimates. Consequently, RANSAC can serve for outlier detection.
- ◆ A basic assumption is that the data consists enough of inliers.

# RANSAC

## [Fischler, Bolles 1981]

- ◆ RANSAC = Random Sampling and Consensus.
- ◆ One of the most cited papers in computer vision.

### In:

$$U = \{x_i\}$$

set of **data points**,  $|U| = N$

$$f(S): S \rightarrow p$$

function  $f$  computes **model parameters**  $p$   
given a sample  $S$  from  $U$

$$\rho(p, x)$$

the **cost function** for a single data point  $x$

### Out:

$$p^*$$

$p^*$ , parameters of the model  
maximizing the cost function

# RANSAC algorithm

$k := 0$

Repeat until  $P\{\text{better solution exists}\} < \eta$  (a function of  $C^*$  and number of steps  $k$ )

$k := k + 1$

## I. Hypothesis

(1) select randomly set  $S_k \subset U$ ,  $|S_k| = m$

(2) compute parameters  $p_k = f(S_k)$

## II. Verification

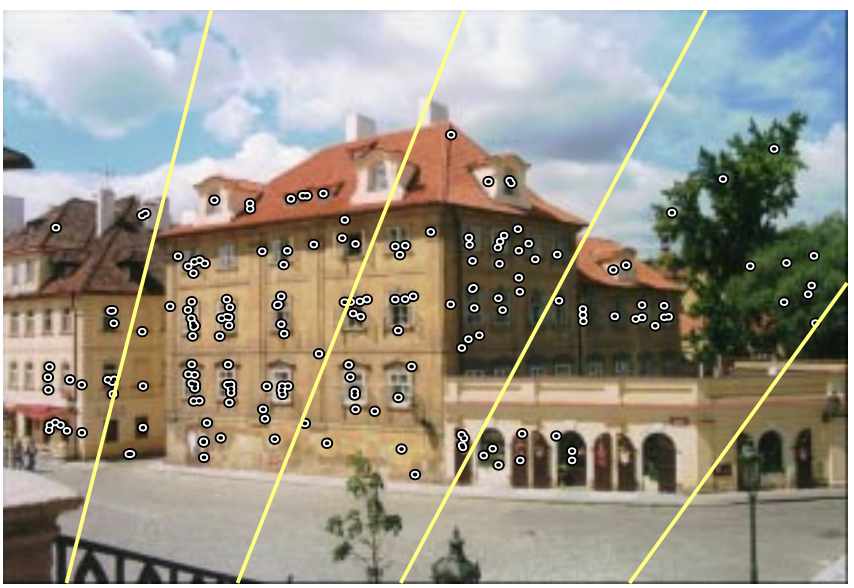
(3) compute cost  $C_k = \sum_{x \in U} \rho(p_k, x)$

(4) if  $C^* < C_k$  then  $C^* := C_k$ ,  $p^* := p_k$

end

# Example I: Epipolar geometry estimation by RANSAC

- ◆ Data points  $U$ : a set of correspondences, i.e., pairs of 2D points
- ◆ Sample size  $m = 7$
- ◆ Model parameters  $f$ : seven-point algorithm - gives 1 to 3 independent solutions
- ◆ Cost function  $\rho$ : thresholded Sampson's error



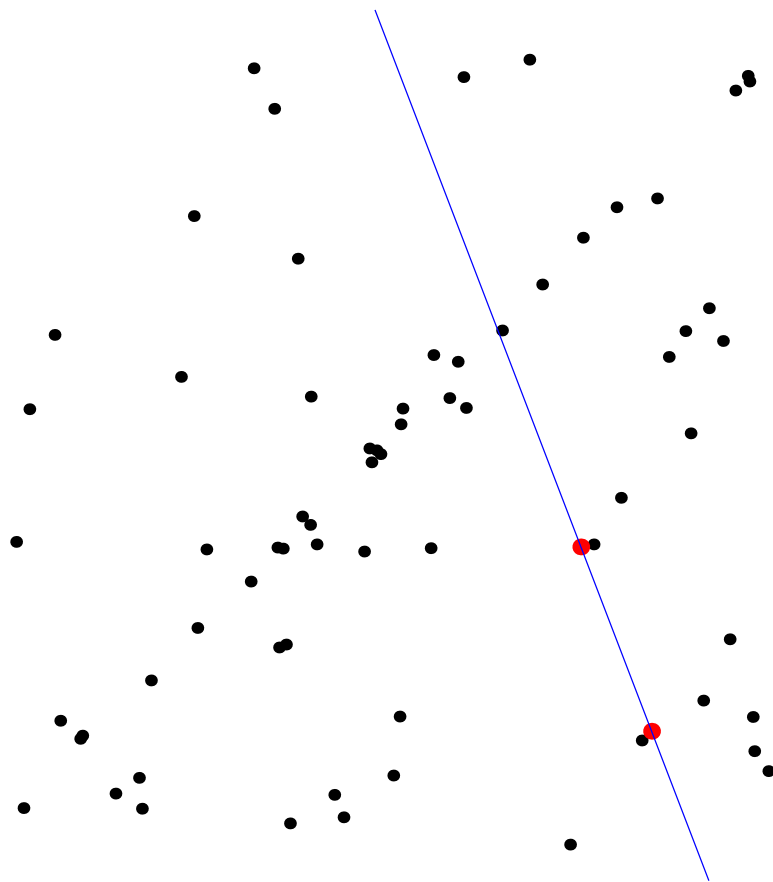
## Example II: Line detection by RANSAC.



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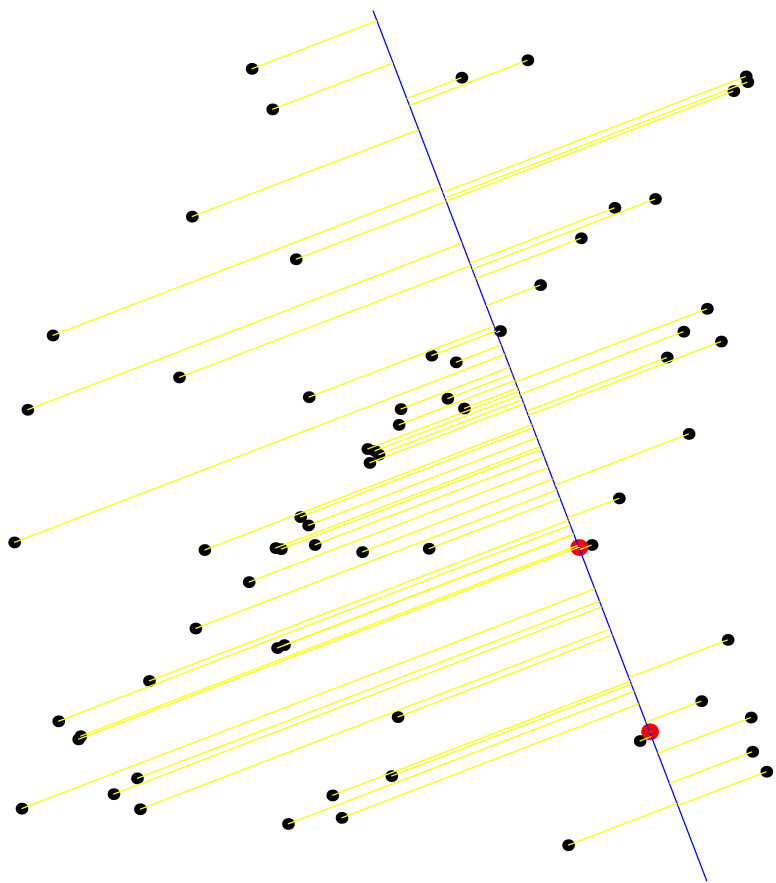


## Example II: Line detection by RANSAC.



- ◆ Select randomly two points.
- The hypothesised model is the line passing through the two points.

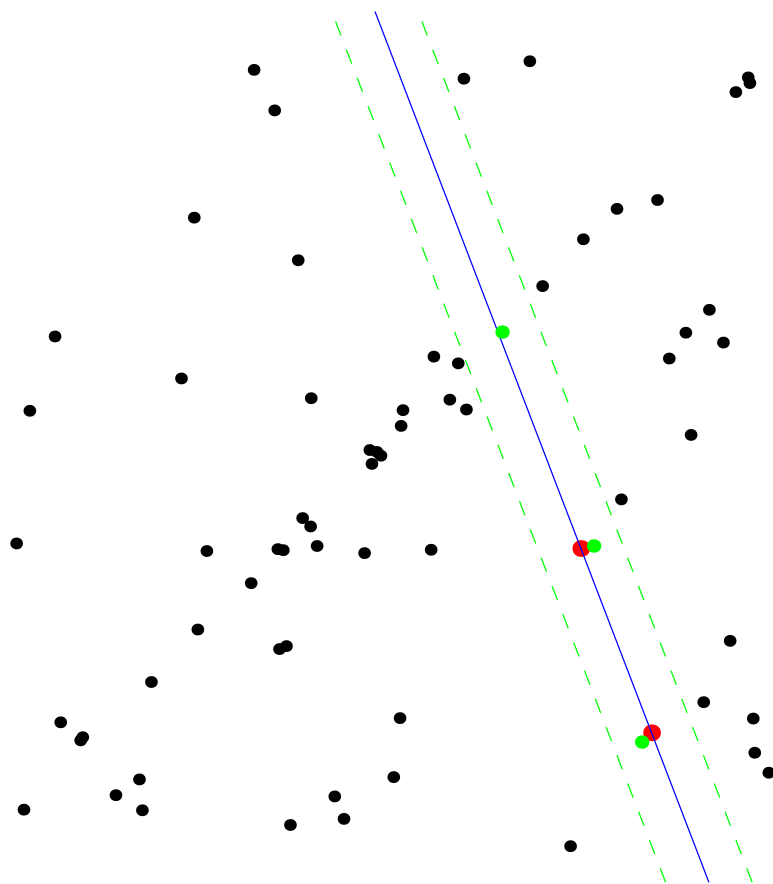
## Example II: Line detection by RANSAC.



- ◆ Select randomly two points.
- ◆ The hypothesised model is the line passing through the two points.
- The error function is a distance from the line.

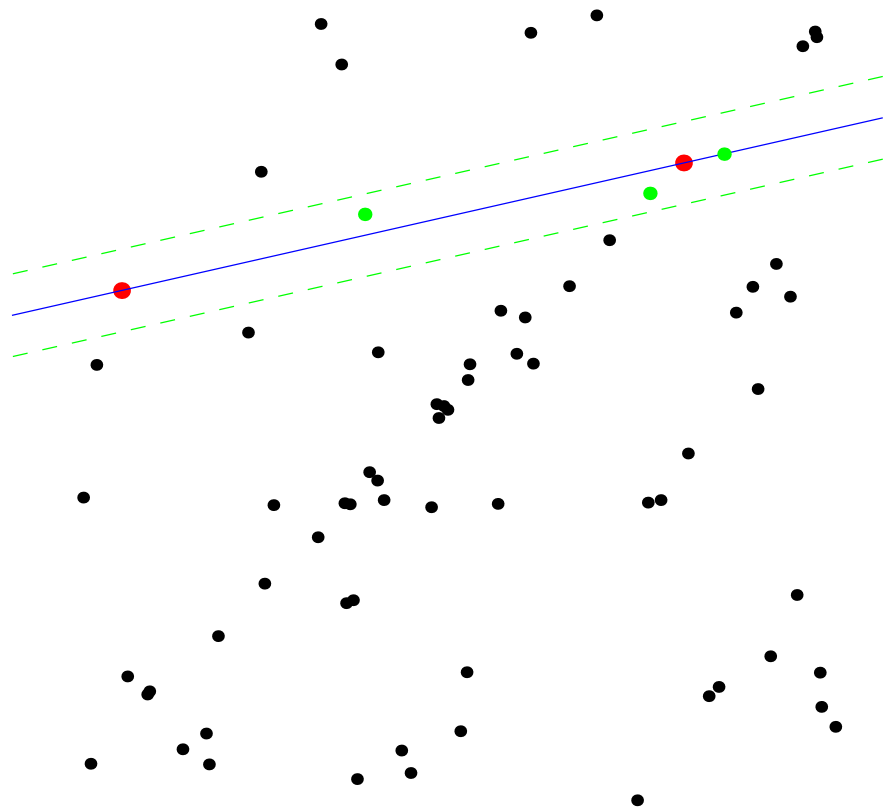


## Example II: Line detection by RANSAC.

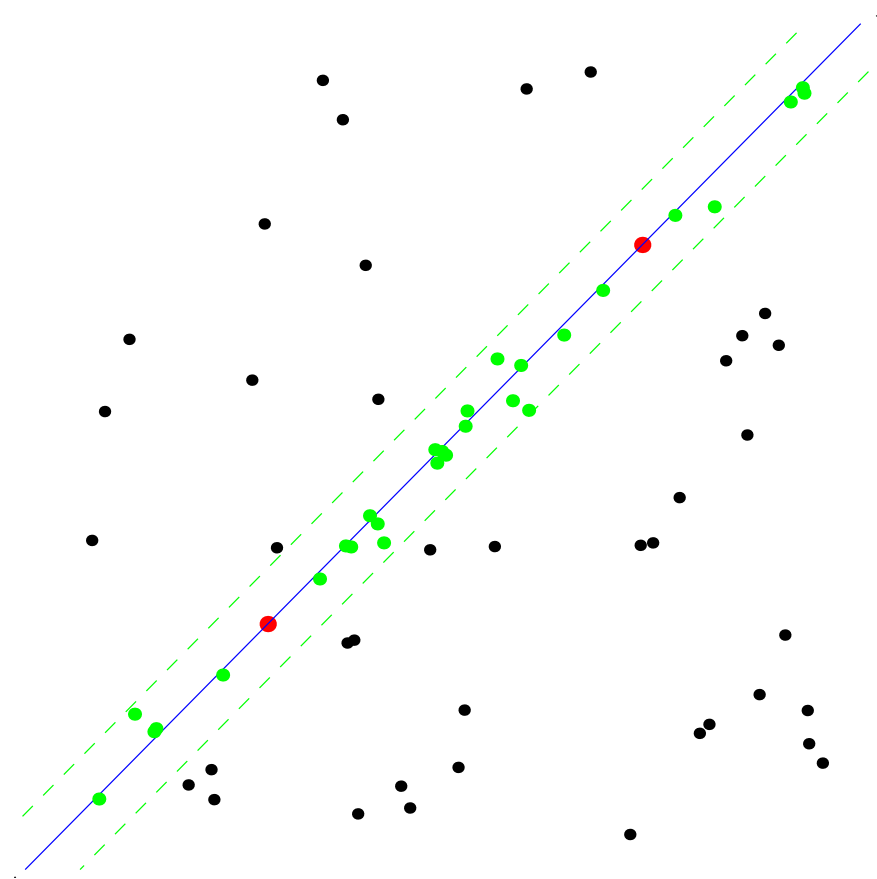


- ◆ Select randomly two points.
- ◆ The hypothesised model is the line passing through the two points.
- ◆ The error function is a distance from the line.
- Points consistent with the model.

# Example II: Line detection by RANSAC.



# RANSAC Time Complexity

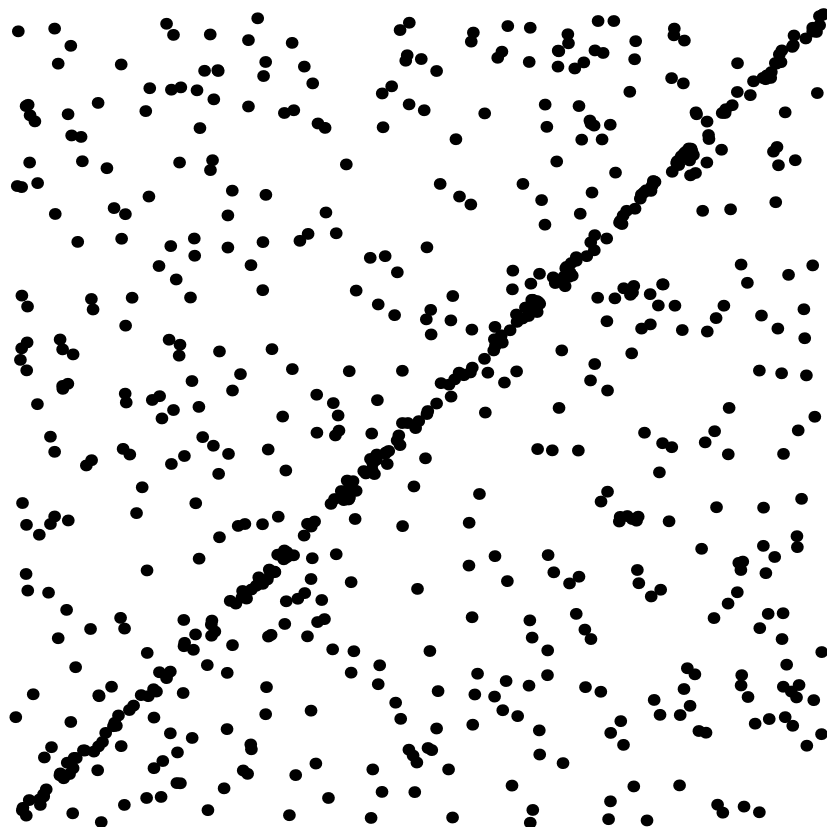


Uncontaminated sample

RANSAC time:  $J = k(t_M + N)$

- ◆  $N$  - number of data points
- ◆  $\epsilon$  - fraction of inliers
- ◆  $m$  - size of the sample
- ◆  $\epsilon^m$  - probability that uncontaminated sample is selected
- ◆  $k = 1/\epsilon^m$  - the average number of samples before uncontaminated one
- ◆  $t_M$  - time to calculate the model

## Number of Data Points



- ◆ For each hypothesised model, all the data points are verified.
- ◆ The more data points the longer RANSAC takes.
- ◆ The majority of samples are contaminated.

### Solution:

- **Randomize** the verification